

Multiple Beta t -Tests of Differential Transcription of mRNAs Between Two Conditions with Small Samples

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Abstract

A major task in the analysis of count data of **RNA** reads from **RNA-Seq** is the detection of differentially expressed genes or isoforms. The count data are presented as a matrix consisting of **RNA** isoform annotation and the number of reads. Analogous analyses also arise for other assay types, such as comparative **ChIP-Seq**. The *MBttest* provides a powerful method to test for differential expression by use of the beta distribution and gene- or isoform-specific variable ρ to control fudge effect due to small sample size.¹ This vignette explains the use of the package. For more detail of the statistical method, please see our paper [8].

Contents

1	Introduction	2
2	Data Preparation and Input	2
3	Simulation for Calculating <i>omega</i> Value	3
3.1	Step1: Simulate null count data	3
3.2	Step2: Perform multiple beta t-tests	4
3.3	Step3: Calculate <i>omega</i> value.	4
4	Normalize the count data	8
5	Perform Multiple Beta t -Tests on The Real Data	8
6	Session Info	14

¹Other Bioconductor packages with similar aims are *edgeR*, *baySeq*, *DESeq* and *DESeq2*

1 Introduction

This vignette is intended to give a rapid introduction to the commands used in implementing new beta t -test methods of evaluating differential expression in high-throughput sequencing data by means of the *MBttest* package. For fuller details on the methods being used, consult Tan et al (2015) [8].

We assume that we have count data from a set of sequencing or other high-throughput experiments, arranged in an array such that except gene annotation information and `id`, each column describes a library and each row describes RNA tag or isoform for which data have been acquired. For example, the rows may correspond to the different sequences observed in a sequencing experiment. The data then consists of the number of each sequence observed in each sample. We wish to determine which, if any, rows of the data correspond to some patterns of differential expression across the samples.

The *MBttest* uses new beta t -test method to identify differential expression for each row. This approach introduces a gene- or isoform-specific variable, called ρ , into t -statistics to control fudge effect resulted from small samples. It has higher work efficiency than existing methods for identifying differential expressions of genes or isoforms either by inflating t -values with $\rho > \omega$ a threshold or by shrinking those with $\rho < \omega$ [8] when number of replicate libraries in each condition is small, for example, equal to or less than 6.

Different from the exiting methods such as *baySeq* [2], *edgeR* Exact test [6] and [7], *edgeR* GLM [5] and [7], *DESeq* [1] and *DESeq2* [4], etc, *MBttest* requires performance of simulation to determine threshold ω before running program *mbetattest*. *MBttest* provides negative binomial simulation program to generate null count data without inputting arguments. User should repeat five or more simulations, perform program *smbettest* to produce null results and calculate ω using the method given in our paper [8].

2 Data Preparation and Input

We begin by loading the *MBttest* package.

```
> library(MBttest)
```

MBttest requires data file contain two parts: Annotation information and count data. Information consists of `tagid`, `geneid`, gene name, chromosome `id`, DNA strand, etc. Information columns are in left side. The count datasheet has at least one column for `geneid` or `tagid` (`isoformid`). The data contain two conditions each having several replicate libraries and must be in right side. Here is an example :

```
> data(jkttcell)
> jkttcell[1:10,]
```

	tagid	geneid	name	chr	strand	pos	anno	Jurk.NS.A	Jurk.NS.B	Jurk.NS.C
1	54	58998	COMT	chr22	+	19956542	sg	66.80	43.48	4.65
2	111	59029	CRKL	chr22	+	21308033	tu-ce	68.75	63.94	66.46
3	171	59104	SLC2A11	chr22	+	24227723	sg	2.86	2.67	8.15
4	231	59157	ADRBK2	chr22	+	26118985	tu	12.88	8.45	8.59
5	242	59164	SRRD	chr22	+	26887904	sg	62.54	59.88	83.27
6	265	59184	HSCB	chr22	+	29153206	tu	4.02	2.07	6.85
7	306	59209	UCRC	chr22	+	30165939	sg	516.71	594.71	83.84
8	327	59212	MTMR3	chr22	+	30426495	tu	4.08	3.99	2.93

Multiple Beta t -Tests of Differential Transcription of mRNAs Between Two Conditions with Small Samples

9	445	59310	NCF4	chr22	+	37274056	sg	0.00	1.30	0.03
10	472	59321	CYTH4	chr22	+	37711384	sg	4.40	1.60	0.12
			Jurk.48h.A	Jurk.48h.B	Jurk.48h.C					
1		32.99		25.49		14.68				
2		80.42		63.89		72.48				
3		12.95		12.70		8.81				
4		13.13		35.34		9.78				
5		54.99		51.15		66.61				
6		9.66		4.02		5.87				
7		254.81		142.26		156.72				
8		10.38		14.23		6.85				
9		71.26		25.89		11.73				
10		37.61		18.54		16.64				

User also may use R function (head) to display the data with top 6 lines:

```
> head(jkttcell)
```

	tagid	geneid	name	chr	strand	pos	anno	Jurk.NS.A	Jurk.NS.B	Jurk.NS.C
1	54	58998	COMT	chr22	+	19956542	sg	66.80	43.48	4.65
2	111	59029	CRKL	chr22	+	21308033	tu-ce	68.75	63.94	66.46
3	171	59104	SLC2A11	chr22	+	24227723	sg	2.86	2.67	8.15
4	231	59157	ADRBK2	chr22	+	26118985	tu	12.88	8.45	8.59
5	242	59164	SRRD	chr22	+	26887904	sg	62.54	59.88	83.27
6	265	59184	HSCB	chr22	+	29153206	tu	4.02	2.07	6.85
			Jurk.48h.A	Jurk.48h.B	Jurk.48h.C					
1		32.99		25.49		14.68				
2		80.42		63.89		72.48				
3		12.95		12.70		8.81				
4		13.13		35.34		9.78				
5		54.99		51.15		66.61				
6		9.66		4.02		5.87				

If the datasheet is .csv file, user can use R function (read.csv) to input data into *R Console* or *RStudio*. If the datasheet is txt file, user can use R function `read.delim` or `read.table` to load data into *R Console* or *RStudio*. After loading data, user should check the data inputted. `jkttcell` shows an example. In this example, 7 columns in the left side are information for *poly(A)* sites. The count data are listed in the right side.

3 Simulation for Calculating *omega* Value

Before performing `mbetatest` on the real data, user needs simulation to determine ω value. There are three steps for doing so:

3.1 Step1: Simulate null count data

Use the following function to generate null simulation data

```
simulat(yy, nci, r1, r2, p, q, A)
```

Multiple Beta t -Tests of Differential Transcription of mRNAs Between Two Conditions with Small Samples

where

yy is real data.

$r1$ and $r2$ are replicate numbers in conditions 1 and 2.

p is proportion of genes differentially expressed in m genes, default value is 0.

q is proportion of genes artificial noise. Its default value is 0.

A is effect value. Its default value is 0. nci : column number of information of data.

Here is an example:

```
> sjknull1<-simulat(yy=jkttcell[1:500,], nci=7,r1=3,r2=3,p=0, q=0.2)
```

The example dataset is *jkttcell*. It has 7 columns for alternative *poly(A)* site information. Two conditions are resting and stimulation. Each has 3 replicate libraries, $r1=3$ and $r2=3$. Since this is null simulation, we set $p=0$ and $q=0.2$ for artificial noise. With the same read data and parameters, you can generate a set of 4-6 null datasets: *sjknull2*, ..., *sjknull6* for calculating ω value.

3.2 Step2: Perform multiple beta t -tests

Use function `smbetatest` to perform multiple beta t -test with $\rho = 1$ on the simulated null data:

```
smbetatest(X, na, nb,alpha)
```

where

X =simulated data.

na and nb are numbers of replicate libraries in conditions 1 and 2.

$alpha$ is probabilistic threshold. User can set $alpha=0.05$ or 0.01 .

The example is

```
> mysim1<-smbetatest(X=sjknull1,na=3,nb=3,alpha=0.05)
```

Save them to .csv files using `write.csv`. After performing `smbetatest` on each simulated null dataset, user would have results recorded in a file like *simulatedNullData1Result.csv* and open it with excel.

In symbol column, `mbeta` t -test gives test result: *sybm* = "-" means that a gene or a tag is not chosen while *sybm* = "+" indicates that the gene or isoform is found to be differentially expressed.

In this example, 12 genes would be found to be falsely positive.

3.3 Step3: Calculate *omega* value

Here is a demo for calculating *omega* (since we can't use greek letter *omega* in R function, we use W to represent *omega*). In Figure 3, red highlighted column is *rho* column. We copied the ρ values of these 12 genes into another empty column and sorted them from the smallest to the largest. Then we gave sequence numbers from 1 to 12 corresponding to ρ -values and calculate q -value for each ordered ρ value:

We chose the 10th ρ value (1.09166) as the first W value because the 11th ρ value has q -value > 0.85 . Repeat this process in 4-6 simulated null datasets and we took the averaged W value as ω value in the real data.

Multiple Beta *t*-Tests of Differential Transcription of mRNAs Between Two Conditions with Small Samples

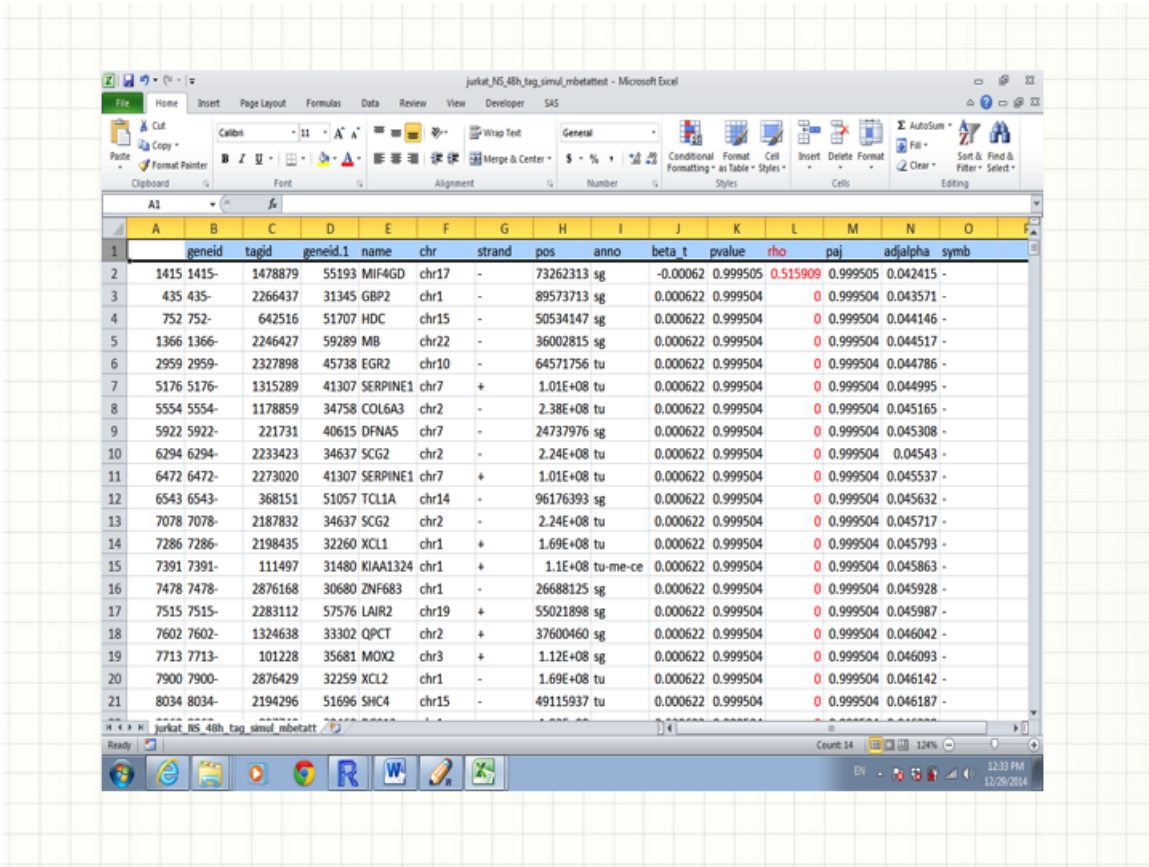


Figure 1: This is an example showing the results obtained by `smbetatetest` from simulated null data. Column A is row number, `geneid` is set in simulation, and `geneid.1` is original `geneid`.

Multiple Beta *t*-Tests of Differential Transcription of mRNAs Between Two Conditions with Small Samples

	E	F	G	H	I	J	K	L	M	N	O	P
13395	37126	INTS12	chr4	-	1.1E+08	sg	-1.94354	0.05195	0.80235	0.05641	0.05	-
13396	48100	CCDC84	chr11	+	1.2E+08	tu	1.94994	0.05118	1.26307	0.05572	0.05	-
13397	55001	TMEM49	chr17	+	5.8E+07	sg	-1.95319	0.0508	0.90153	0.05538	0.05	-
13398	58378	KIAA0611	chr20	-	5E+07	sg	-1.95439	0.05065	0.68436	0.05531	0.05	-
13399	34138	PRPF40A	chr2	-	1.5E+08	tu	-1.9725	0.04855	0.73165	0.0531	0.05	+
13400	51790	RAB27A	chr15	-	5.5E+07	tu	-1.98929	0.04667	0.99629	0.05114	0.05	+
13401	55677	PSTPIP2	chr18	-	4.4E+07	sg	2.0056	0.0449	0.79744	0.0493	0.05	+
13402	37611	SAKI	chr5	-	6599356	sg	2.16009	0.03077	0.8255	0.03386	0.05	+
13403	48862	CSRNP2	chr12	-	5.1E+07	tu	2.17827	0.02939	0.81415	0.03243	0.05	+
13404	42480	CPNE3	chr8	+	8.8E+07	tu	-2.24952	0.02448	0.76494	0.0271	0.05	+
13405	51646	ELL3	chr15	-	4.4E+07	sg	-2.26327	0.02362	1.09165	0.02625	0.05	+
13406	39328	HLA-DPA1	chr6	-	3.3E+07	sg	2.3214	0.02027	1.11709	0.02262	0.05	+
13407	31360	ZNF644	chr1	-	9.1E+07	tu	-2.35636	0.01846	0.91156	0.02073	0.05	+
13408	42490	DECR1	chr8	+	9.1E+07	sg	2.41858	0.01558	0.89546	0.01765	0.05	+
13409	59372	LGALS1	chr22	+	3.8E+07	sg	2.81137	0.00493	1.035	0.00566	0.05	+
13410	50230	ATP11A	chr13	+	1.1E+08	tu-ce	-3.15317	0.00162	1.35415	0.0019	0.05	+
13411												

Figure 2: The row number in column A in Figure 1 was deleted. To show explicitly, we here hid `geneid` (for simulation), `tagid` column and selected rows are genes that were identified to be differentially expressed.

Multiple Beta *t*-Tests of Differential Transcription of mRNAs Between Two Conditions with Small Samples



Figure 3: Demo for calculating *W*

4 Normalize the count data

As a second processing step, we need to estimate the effective library size. This step is also called *normalization*, even though it may not make the count data be of normal distribution. If the counts of expressed genes in one condition are, on average, twice as high as in another (because the library was sequenced twice as deeply), the size factor for the first condition should be twice higher than the second one, then differential analysis would give error results. For this reason, we must make all libraries have the same size before performing any statistical method. For doing so, user can the function `estimateSizeFactors` of package **DESeq** [1] or `textbfDESeq2` [4] to estimate the size factors from the count data or use the following simple method to normalize the the count data: In excel sheet, use function `sum` to calculate sizes of all libraries, and then use excel function `average` to calculate averaged library size. The last step is to use the following equation to convert the original count data to new count data with the same library size:

$$Y_{ik} = \frac{y_{ij} \bar{N}}{N_j} \quad \begin{matrix} 1 \\ 2 \end{matrix}$$

where

$i = 2, \dots, n$ (number of genes or isoforms) in rows in a sheet, $j = nci + 1, \dots, nci + c$ where $c = na + nb$ and nci is column number of annotation information; $k = nci + c + 2 + j$; N_j is size of library j and \bar{N} is mean of sizes over all libraries; y_{ij} is original count of RNA reads in row i and column j .

5 Perform Multiple Beta t -Tests on The Real Data

Suppose the data have been normalized so that all libraries have the same size. After obtaining W value, user can use the function and the real data to perform `mbeta t-test`: `mbetat test(X, na, nb, W, alpha, file)` where X is real data. In our current example, $X = jktcell$. na and nb are respectively numbers of replicate libraries in conditions 1 and 2. For `jktcell` data, $na = nb = 3$. W is omega value. According to our calculation above step, $W = 1$. $alpha$ is the probabilistic threshold. You can set $alpha = 0.05$ or 0.01 or the other values; `file` is `csv` file for saving the results. The example is

```
> res<-mbetat test(X=jktcell[1:1000,], na=3, nb=3, W=1, alpha=0.05, file="jurkat_NS_48h_tag_mbetat test.csv")
```

`mbetat test` has two output results: one is saved in `csv` file and the other is `dat` for `maplot` and for `heatmap`. The package `MBttest` has this result obtained the whole data. We here load it for making `MAplot`:

```
> data(dat)
> head(dat)
```

	tagid	geneid	name	chr	strand	pos	anno	Jurk.NS.A	Jurk.NS.B	Jurk.NS.C	Jurk.48h.A
1	83344	58782	MX1	chr21	+	42831139	sg	0	0.00	0.00	29.61
2	197313	56792	CD22	chr19	+	35838262	sg	0	0.45	3.81	96.33
3	202264	53072	CD19	chr16	+	28950664	sg	0	0.00	0.00	37.65
4	232007	37653	BASP1	chr5	+	17276943	sg	0	0.55	1.31	63.15
5	301820	46661	HBB	chr11	-	5246697	sg	0	0.00	0.00	4.52
6	368151	51057	TCL1A	chr14	-	96176393	sg	0	1.03	5.15	153.51

Multiple Beta t -Tests of Differential Transcription of mRNAs Between Two Conditions with Small Samples

	Jurk.48h.B	Jurk.48h.C	beta_t	rho	symp
1	0.48	0	0	0	-
2	8.07	0	0	0	-
3	0.52	0	0	0	-
4	0.58	0	0	0	-
5	39.52	0	0	0	-
6	9.93	0	0	0	-

```
> maplot(dat=dat,r1=3,r2=3,TT=350,matitle="MA plot")
```



Figure 4: 'MA'-plot of t -value against log mean over all replicate libraries across two conditions. The iso-forms who were given differential transcripts in simulation had absolute larger t -values that were highlighted in red than the threshold given in multiple tests. Those who were given no differential expression had very small absolute t -values close to zero labeled in black across long means. Here threshold for truncating t -values is set to be 350, since none of absolute t -values are over 350, the *MAplot* is an outline *MAplot* in which red and black dots are not explicitly seen.

```
> maplot(dat=dat,r1=3,r2=3,TT=50,matitle="MA plot")
```

myheatmap has multiple options: both-side, row and column cluster trees with distance methods: "euclidean", "pearson", "spearman", and "kendall" correlation coefficients and color label with "redgreen", "greenred", "redblue", "bluered" or "heat.colors" and angles for genes or isoforms in row and cases (conditions) in column. User can use default without any



Figure 5: 'MA'-plot of t -value against log mean over all replicate libraries across two conditions. To explicit display the t -values across log mean, absolute t -values ≥ 50 were truncated. One can explicitly see that truly differential transcripts in simulation had absolute larger t -values that were highlighted in red than the threshold given in multiple tests and those who had no differential expressions had very smaller absolute t -values that were labeled in black than the threshold.

choice like (Figure 6) which has `tree="both"` for both-side tree, or choose `tree="column"` like (Figure 8) if columns are species or cancer cases or not choose tree with `tree="none"` (see (Figure 7)). User may change `heatmap` color with `colors`, for example, in (Figure 8), we chose `colors="redblue"`. If user find that default column name or row name does no have good angles, then user can adjust them with `rwangle` (row angle) or `clangle`(column angle). `rwangle` and `clangle` values are from 0 to 90.

```
> myheatmap(dat=dat, r1=3, r2=3, maptitle="Jurkat T-cell heatmap2")
```

```
> myheatmap(dat=dat, r1=3, r2=3, tree="none", maptitle="Jurkat T-cell heatmap3")
```

```
> myheatmap(dat=dat, r1=3, r2=3, colors="redblue", tree="column",
+ method="pearson", maptitle="Jurkat T-cell heatmap")
```

Multiple Beta t -Tests of Differential Transcription of mRNAs Between Two Conditions with Small Samples

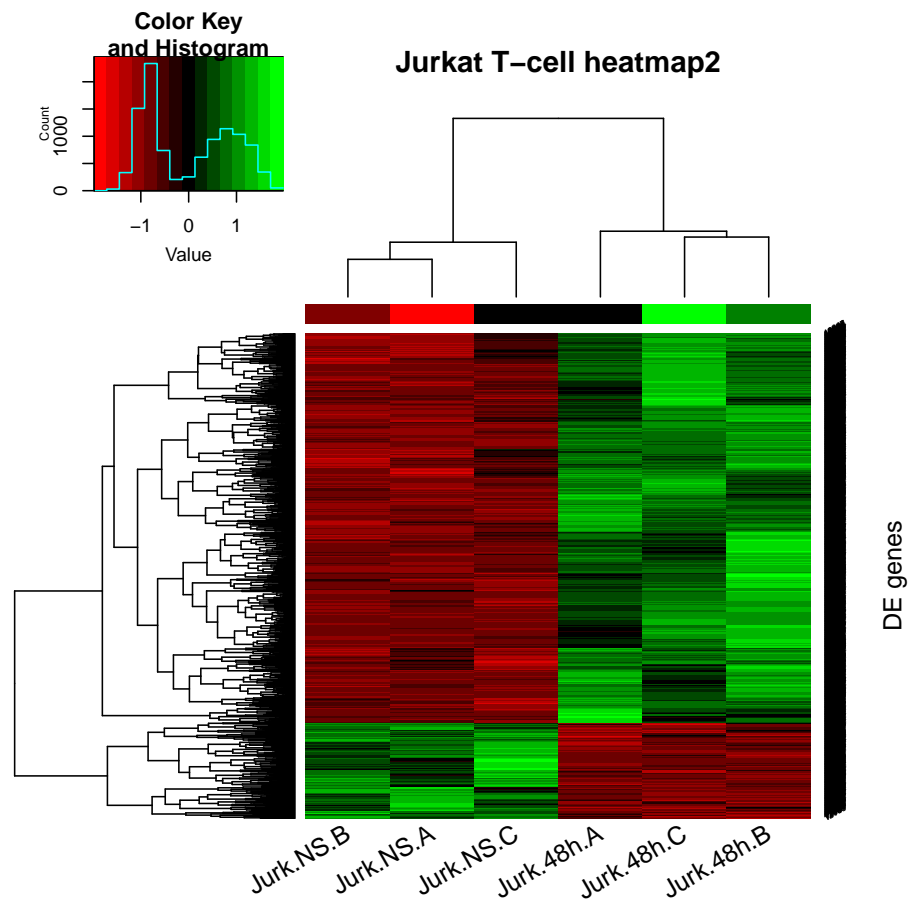


Figure 6: The *heatmap* has both-side trees and displays explicitly differential expression between stimulating and rest. Most of genes were up-expressed by stimulation but a small part of genes were down-expressed. The tree in column divides columns into two groups: NS and 48h. The tree in row is tree of differentially expressed genes and also divide genes in row into two big groups.

Multiple Beta *t*-Tests of Differential Transcription of mRNAs Between Two Conditions with Small Samples



Figure 7: The *heatmap* did not give trees on both sides, but the *heatmap* is the same with (Figure 6)

Multiple Beta t -Tests of Differential Transcription of mRNAs Between Two Conditions with Small Samples

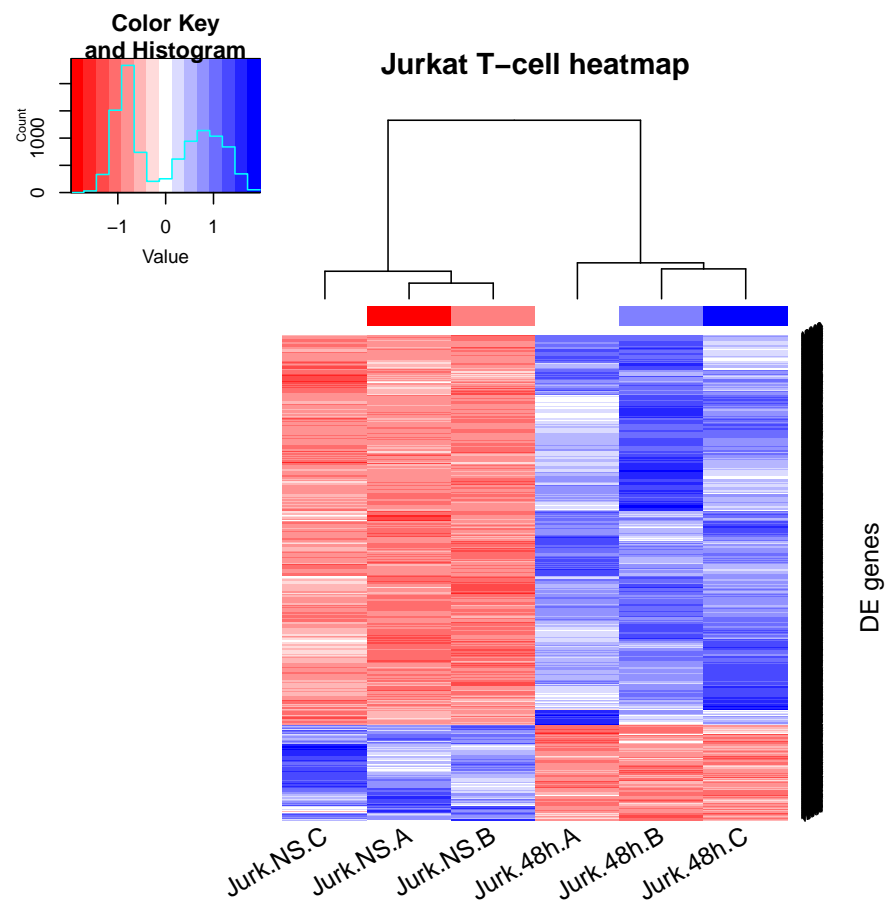


Figure 8: This *heatmap* was labeled with red and blue and gave column trees

6 Session Info

```
> sessionInfo()

R Under development (unstable) (2025-03-01 r87860 ucrt)
Platform: x86_64-w64-mingw32/x64
Running under: Windows Server 2022 x64 (build 20348)

Matrix products: default
  LAPACK version 3.12.0

locale:
 [1] LC_COLLATE=C                      LC_CTYPE=English_United States.utf8
 [3] LC_MONETARY=English_United States.utf8 LC_NUMERIC=C
 [5] LC_TIME=English_United States.utf8

time zone: America/New_York
tzcode source: internal

attached base packages:
 [1] stats      graphics  grDevices  utils      datasets  methods   base

other attached packages:
 [1] MBttest_1.35.0 gtools_3.9.5  gplots_3.2.0

loaded via a namespace (and not attached):
 [1] digest_0.6.37      fastmap_1.2.0      xfun_0.51           KernSmooth_2.23-26
 [5] knitr_1.50         htmltools_0.5.8.1  rmarkdown_2.29      bitops_1.0-9
 [9] cli_3.6.4          caTools_1.18.3     compiler_4.5.0      tools_4.5.0
[13] evaluate_1.0.3     yaml_2.3.10        BiocManager_1.30.25 rlang_1.1.5
[17] BiocStyle_2.35.0
```

References

- [1] Anders S, Huber W (2010) *Differential expression analysis for sequence count data*. Genome Biol 11: R106.
- [2] Thomas J. Hardcastle and Krystyna A. Kelly (2010) *baySeq: Empirical Bayesian Methods For Identifying Differential Expression In Sequence Count Data*. BMC Bioinformatics.
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- [4] Love MI, Huber W, Anders S (2014) *Moderated estimation of fold change and dispersion for RNA-Seq data with DESeq2*. bioRxiv doi:10.1101/002832.
- [5] McCarthy DJ, Chen Y, Smyth GK (2012) *Differential expression analysis of multifactor RNA-Seq experiments with respect to biological variation*. Nucleic Acids Res, 2012, 40: 4288-4297.

Multiple Beta t -Tests of Differential Transcription of mRNAs Between Two Conditions with Small Samples

- [6] Robinson MD, Smyth GK (2008) *Small-sample estimation of negative binomial dispersion, with applications to SAGE data*. Biostatistics 2008, 9: 321-332.
- [7] Robinson MD, McCarthy DJ, Smyth GK (2010) *edgeR: a Bioconductor package for differential expression analysis of digital gene expression data*. Bioinformatics 26: 139-140.
- [8] Yuan-De Tan, Anita M. Chandler, Arindam Chaudhury, and Joel R. Neilson(2015) *A Powerful Statistical Approach for Large-scale Differential Transcription Analysis*. Plos One. 2015 DOI: 10.1371.